EXAM FUNCTIONAL PROGRAMMING

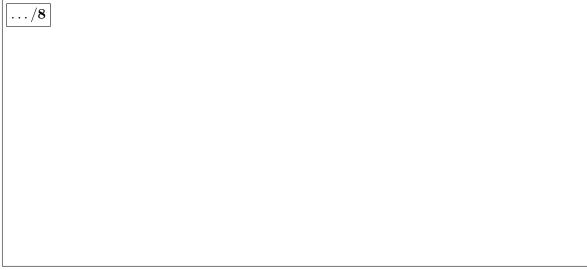
Tuesday th	ne 29th of September 2015, 11.00 h 13.00 h.
Name: Student n	number:
explain you is the (one and explan At the end correctness by 10 to ob. In any functions/conot, (.), ele	begin: Do not forget to write down your name and student number above. If necessary, ar answers (in English or Dutch). For multiple choice questions, clearly circle what you think and only) best answer. Use the empty boxes under the other questions to write your answer ations in. Use the blank paper provided with this exam only as scratch paper (kladpapier). It of the exam, only hand in the filled-in exam paper. Answers will not only be judged for a but also for clarity and conciseness. A total of one hundred points can be obtained; divide otain your grade. Good luck! of your answers below you may (but do not have to) use the following well-known Haskell operators: replicate, id, concat, foldr (and variants), map, filter, const, all, any, flip, fst, snd, em, take, drop, take While, drop While, head, tail, (++), lookup, max, min and all members a classes Eq, Num, Ord, Show and Read.
	Write a function $allNats :: [Int] \rightarrow Bool$ that returns $True$ if and only if all values in the input list are larger than zero. You are not allowed to use explicit recursion. $/6$
]	Using explicit recursion (no higher-order functions!) implement the function $pairUp$ that pairs subsequent elements of a list: $pairUp$ [1, 2, 3, 4] returns [(1, 2), (3, 4)]. If the list has an odd number of elements, the final element of the list should be $ignored$. So $pairUp$ [1, 2, 3, 4, 5] is also [(1, 2), (3, 4)]. /8

(iii) The function *rldecode* performs run length decoding. For the input [1,2,3,4] we expect it to generate the list [2,4,4,4]: the first number tells us how many of the second end up in the output, the third number says how many of the fourth we want, and so on. If the input list contains negative numbers or zero, then the empty list should be returned.

We implement this function using the functions allNats and pairUp as follows:

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\begin{array}{l} rldecode :: [\mathit{Int}] \longrightarrow [\mathit{Int}] \\ rldecode \ xs = \\ & \textbf{if} \ all Nats \ xs \ \textbf{then} \\ & foldr \ f \ e \ arg \\ & \textbf{else} \\ & [] \\ & \textbf{where} \ f \ \dots \\ & e \ \dots \\ & arg \ \dots \end{array}
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Given suitable definitions for f, e and arg.



(iv) Give the type of the function flip that when given an arbitrary binary function f, returns the function that takes the arguments for f in reverse order.

$\lfloor \dots /5 \rfloor$		

2. (i)	Define a datatype CountTree a with the following properties: a. the leaves of the tree do not contain any information b. in the branches, the tree splits in two c. in every branch there is a piece of information of (the same) type a, and d. in every branch there is an additional value of type integer
	/7
(ii)	Write a function
	$height:: Count Tree\ a \rightarrow Int$ that computes how high the tree is. The height of a $Leaf$ is zero, the height of a non-leaf is one more than the maximum height of the subtrees.
	/7
(iii)	Write a function insert:: Float -> CountTree Float -> CountTree Float that adds an element to a count tree, even if it is already present. The function may assume the tree has the following properties, but must also ensure that the tree that it returns has those same properties: (A) the values in the branches are in order, meaning that the value in a node is larger then or equal to the values in the left subtree, and smaller than all the values in the right subtree. (B) the additional integer values indicate how many values are contained in the LEFT subtree of each node.
	/8

	(iv)	Write a function $insertU$ that behaves almost the same as $insert$ but that only insert the float argument if it does not yet occur in the tree. In your implementation, you may visit every branch at most once. Hint: implement a helper function $insertHelp::\rightarrow (CountTree\ Float,Bool)$ that returns not only the modified tree, but some additional information as well. $\boxed{\ldots/6}$
3.	(i)	A very efficient definition of $segs$ for all segments of a list is $segs \ xs = []: [t \mid i <- inits \ xs, t <- tails \ i, not \ (null \ t)]$ What is $segs \ [1,2,3,4]$? $\boxed{\dots/4}$
	(ii)	Explain in your own words how this function computes what it is supposed to compute. If necessary illustrate by a small example. /6

- 4. [.../20] The following multiple choice questions are each worth 5 points.
 - (i) Let f be any function of type $Int \rightarrow Bool$. Which expression has the same value as the following list comprehension?

$$[f \ x \mid x < -[2..8], odd \ x]$$

- a. filter odd (map f [2..8])
- b. $f (map \ odd \ [2..8])$
- c. map f (filter odd [2..8])
- d. filter f (map odd [2..8])
- (ii) I [id, const 2] is well-typed
 - II $\ x \rightarrow [even \ x, fib \ x]$, where fib is the well-known Fibonacci function, is well-typed
 - a. Both I and II are true
 - b. Only I is true
 - c. Only II is true
 - d. Both I and II are false
- (iii) Given that $until :: (a \rightarrow Bool) \rightarrow (a \rightarrow a) \rightarrow a \rightarrow a$ what is the type of $foldr\ until?$
 - a. $(b \rightarrow Bool) \rightarrow b \rightarrow [b \rightarrow b] \rightarrow b$
 - b. $[a \rightarrow a] \rightarrow [a \rightarrow Bool] \rightarrow [a]$
 - c. $(a \rightarrow a) \rightarrow [a \rightarrow Bool] \rightarrow a \rightarrow a$
 - d. The expression is type incorrect.
- (iv) I In an expression with only associative operators you can omit all parentheses.
 - II That the operator (++) is defined as right-associative helps increase computational efficiency.
 - a. Both I and II are true
 - b. Only I is true
 - c. Only II is true
 - d. Both I and II are false

rse).		
/15		